# **Contrastive Learning** with Adversarial Examples

### Introduction

- Contrastive learning (CL) is one of the popular technique for self-supervised learning (SSL) of visual representations.
- CL treats instances as classes and aims to learn an invariant instance representation.
- This is implemented by generating a pair of examples per instance, and feeding them • through an encoder, which is trained with a constrastive loss.
- The design of positive pairs is one of the research focuses of CL. For example, [1] shows that data augmentation is critical for the success of CL with different augmentation approaches having a different impact on SSL performance.
- While CL resembles metric learning approaches such as noise contrastive estimation [2] and N-pair [3] losses, the design of negative pairs has received less emphasis in the CL literature, unlike the plethora of positive pair selection proposals.
- In this work, we seek a general algorithm for the generation of diverse positive and challenging negative pairs for CL algorithms.
- This is framed as the search for instance augmentation sets that induce the largest optimization cost for CL with adversarial examples
- We show that it is possible to leverage the interpretation of CL as instance classification • to produce a sensible generalization of classification attacks to the CL problem.
- The new attacks are then combined with recent techniques from the adversarial literature which treat adversarial training as multi-domain training.
- We show that the novel procedure Contrastive Learning with Adversarial Examples (CLAE) can boost the performance of several CL baselines across different datasets.

### **Contrastive learning**

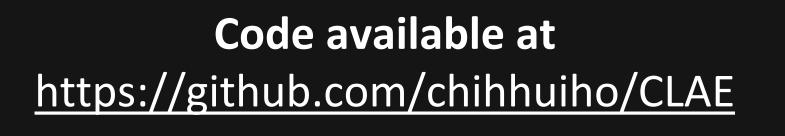
Contrastive learning (CL) is formulated as

$$L_{cl}(x_i^{q_i}, x_i^{p_i}; \theta, \mathcal{T}) = -\log \frac{e^{f_{\theta}(x_i^{q_i})^T f_{\theta}(x_i^{p_i})/\tau}}{\sum_{k=1}^{B} e^{f_{\theta}(x_i^{q_i})^T f_{\theta}(x_k^{p_k})/\tau}} , q_i, p_i \sim \mathcal{T}$$
(1)

where f is an embedding parameterized by  $\theta$ ,  $\tau$  is the temperature, B is the batch size and  $x_i^{p_i}$ ,  $x_i^{q_i}$  are augmentations of  $x_i$  under transformations  $q_i$ ,  $p_i$  randomly sampled from some set of transformations  $\mathcal{T}$ .

- While [12] has shown that the choice of  $\mathcal{T}$  has a critical role on SSL performance, most prior works do not give much consideration to the individual choice of  $q_i$  and  $p_i$ .
- In this work, we seek augmentations that maximize the risk defined by the loss of (1), i.e.  $\{r_i^*, q_i^*\} = \underset{\{r_i, q_i\} \sim \mathcal{T}}{\operatorname{argmax}} \sum_i L_{cl}(x_i^{r_i}, x_i^{q_i}; \theta, \mathcal{T})$
- However, optimizing (2) is difficult. Instead, we proposed to fix the augmentation  $q_i$  and minimize

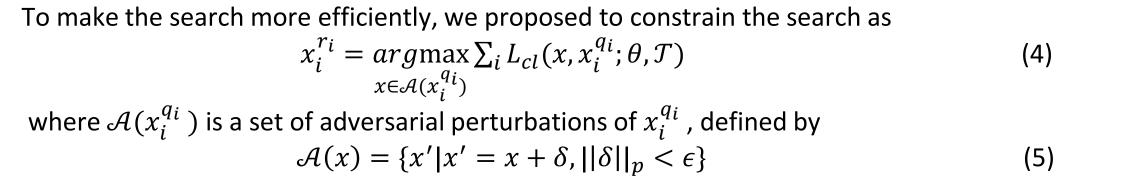
$$\{r_i^*\} = \underset{\{r_i\}\sim\mathcal{T}}{\operatorname{argmax}} \sum_i L_{cl}(x_i^{r_i}, x_i^{q_i}; \theta, \mathcal{T})$$
(3)





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### **Proposed method**



To optimize (4), we reformulate the contrastive loss of (1) as the cross-entropy loss

$$L_{ce}(x_i^{q_i}, i; \{\frac{f_{\theta}(x_k^{p_k})}{\tau}\}, \theta)$$
(6)

where 
$$L_{ce}(x, y; W, \theta) = -log \frac{e^{w_y^r f_{\theta}(x)}}{\sum_k e^{w_k^T f_{\theta}(x)}}$$

Then (4) becomes

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$$\{x_k^{r_k}\} = \underset{\{x \in \mathcal{A}\left(x_i^{q_i}\right)\}}{\operatorname{argmax}} \sum_i L_{ce}(x_i^{q_i}, i; f_{\theta}(x_k) / \tau, \theta) \quad q_i \sim \mathcal{T}$$
(7)

By substitute (5) into (7)

$$\{\delta_k^*\} = \underset{\{\delta_k\}}{\operatorname{argmax}} \sum_i L_{ce}(x_i^{q_i}, i; f_\theta(x_i^{q_i} + \delta_k) / \tau, \theta) \text{ s.t. } ||\delta_k||_p < \epsilon, \quad q_i \sim \mathcal{T}$$
(8)

In this work, we rely on untargeted FGSM [] to solve (8) and compute  $\{x_k^{r_k}\}$  as

$$x_{k}^{r_{k}} = x_{k}^{q_{k}} + \delta_{k}^{*} = x_{k}^{q_{k}} + \epsilon sign(\nabla_{x_{k}^{q_{k}}} \sum_{i} L_{ce}(x_{i}^{q_{i}}, i; f_{\theta}(x_{k}^{q_{k}})/\tau, \theta)), ||\delta_{k}||_{2} < \epsilon$$
(9)

• To perform SSL training, we adopt the training scheme of AdvProp [], which uses two separate batch normalization (BN) layers for clean and adversarial examples.

• The overall loss function contains CL losses computed with augmented examples and adversarial examples and is formulated as

$$\underset{\theta}{\operatorname{argmax}} \sum_{i} L_{ce}(x_{i}^{q_{i}}, i; \{\frac{f_{\theta}(x_{k}^{p_{k}})}{\tau}\}, \theta) + \alpha \sum_{i} L_{ce}(x_{i}^{q_{i}}, i; \{\frac{f_{\theta}(x_{k}^{r_{k}})}{\tau}\}, \theta)$$
(10)

We refer this as Contrastive Learning with Adversarial Example (CLAE) and the procedure of CLAE is summarized in Algorithm 1.

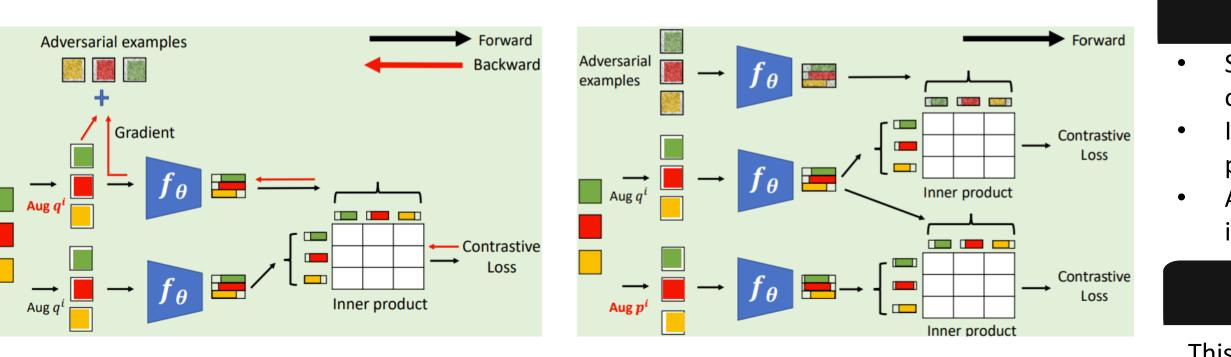
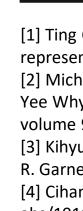


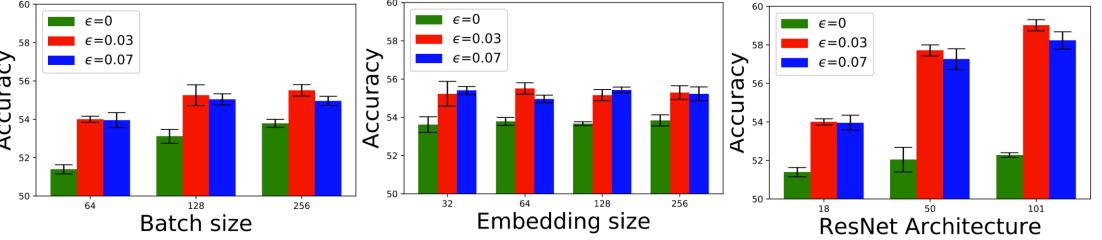
Figure 1. (Left) Generation of adversarial augmentations in step 4 of Algorithm 1 (Right) Adversaria training with contrastive loss in step 5 of Algorithm 1

Algorithm 1 Pseudocode of adversarial training with constrastive loss in a batch

- 1: Input  $\mathcal{X} = \{x_i\}_{i=1}^B$ , AUG:= Data Augmentation, Hyperparameter  $\alpha$
- 2:  $\mathcal{W}^p = \{x_i^{p_i}\}_{i=1}^B = AUG(\mathcal{X})$
- 3:  $\mathcal{W}^q = \{x_i^{q_i}\}_{i=1}^B = AUG(\mathcal{X})$
- 4: Compute (15) with  $\{x_i^{q_i}\}_{i=1}^B$  and  $\mathcal{W}^q$  to obtain  $\mathcal{W}^*$
- 5: Compute  $L_{aug}$  of (16) with  $\{x_i^{q_i}\}_{i=1}^B$  and  $\mathcal{W}^p$ , and  $L_{adv}$  of (16) with  $\{x_i^{q_i}\}_{i=1}^B$  and  $\mathcal{W}^*$
- 6: Minimize (16) with hyperparameter  $\alpha$



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### Experiments

Table 1: Downstream classification accuracy for three SSL methods, with and without ( $\epsilon$ = 0) adversarial augmentation, on different datasets.

		kNN		LR		
Method	$\epsilon$	Cifar10	Cifar100	Cifar10	Cifar100	tinyImageNet
Plain	0	82.78±0.20	54.73±0.20	79.65±0.43	$51.82 \pm 0.46$	31.71±0.23
	0.03	83.09±0.19	55.28±0.12	79.94±0.28	$52.04 {\pm} 0.32$	32.82±0.10
	0.07	$83.04{\pm}0.18$	54.96±0.12	79.85±0.16	52.14±0.21	32.71±0.22
	0	83.63±0.14	55.23±0.28	80.63±0.18	52.99±0.25	$32.32 \pm 0.30$
$_{0.03}^{\text{UEL}}$ [5] $_{0.07}^{0.03}$		84±0.15	55.96±0.06	80.94±0.13	54.27±0.40	33.72±0.30
[	0.07	83.72±0.19	55.36±0.22	$80.82{\pm}0.12$	$53.90 {\pm} 0.11$	33.16±0.36
	0	$75.92{\pm}0.26$	34.94±0.25	83.27±0.17	53.79±0.21	40.11±0.34
SimCLR	<b>1 0</b> .03	$76.45 \pm 0.32$	38.89±0.25	83.32±0.26	$55.52{\pm}0.30$	<b>41.62±0.20</b>
L	0.07	76.70±0.36	$38.41 \pm 0.21$	83.13±0.22	$54.96 {\pm} 0.20$	$41.46 {\pm} 0.22$
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Figure2 Ablation study of (a) batch sizes ,(b) embedding dimensions and (c) ResNet architectures.

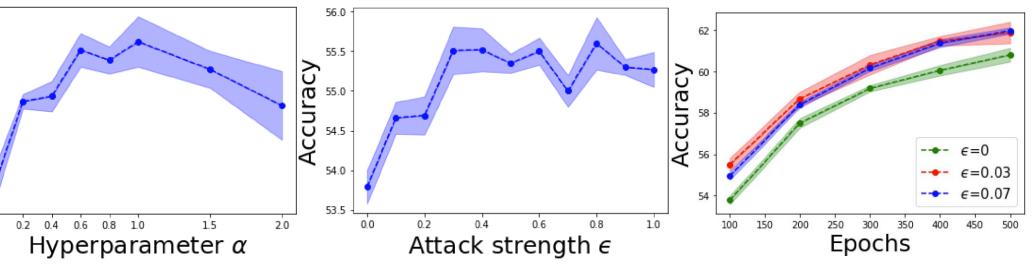


Figure 3: Ablation study for (a) hyperparameter  $\alpha$ , (b) attack strength and (c) longer pretext training.

### Conclusion

Self-supervised learning approaches based on contrastive learning do not necessarily optimize on hard negative pairs.

In this work, we have proposed a new algorithm (CLAE) that generates more challenging positive and hard negative pairs by leveraging adversarial examples.

Adversarial training with the proposed adversarial augmentations was demonstrated to improve performance of several CL baselines.

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